

# Computational Intelligence

Winter Term 2013/14

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### Contents

- Ant algorithms (combinatorial optimization)
- Particle swarm algorithms (optimization in  $\mathbb{R}^n$ )

metaphor

swarms of bird or fish  
seeking for food



concepts:

- **evaluation** of own current situation
- **comparison** with other conspecific
- **imitation** of behavior of successful conspecifics

⇒ audio-visual communication

ants or termites  
seeking for food



concepts:

- communication / coordination by means of „**stigmergy**“
- **reinforcement learning**  
→ positive feedback

⇒ olfactoric communication

### ant algorithms (ACO: Ant Colony Optimization)

paradigm for design of metaheuristics for combinatorial optimization

stigmergy = indirect communication through modification of environment

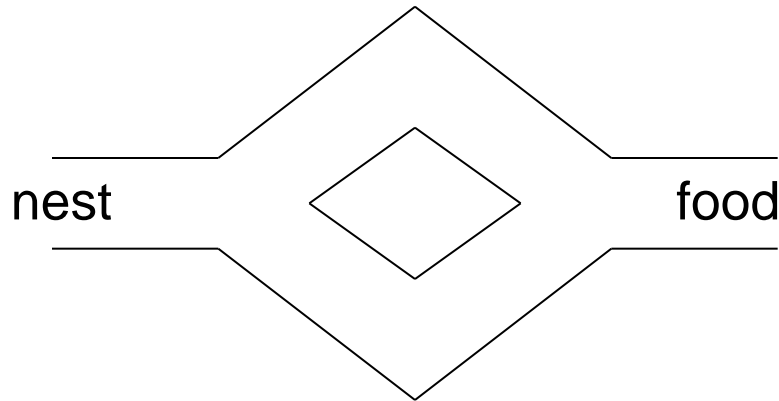
~ 1991 Coloni / Dorigo / Maniezzo: Ant System (also: 1. ECAL, Paris 1991)

Dorigo (1992): collective behavior of social insects (PhD)

### **some facts:**

- about 2% of all insects are social
- about 50% of all social insects are ants
- total weight of all ants = total weight of all humans
- ants populate earth since 100 millions years
- humans populate earth since 50.000 years

**double bridge experiment** (Deneubourg et al. 1990, Goss et al. 1989)

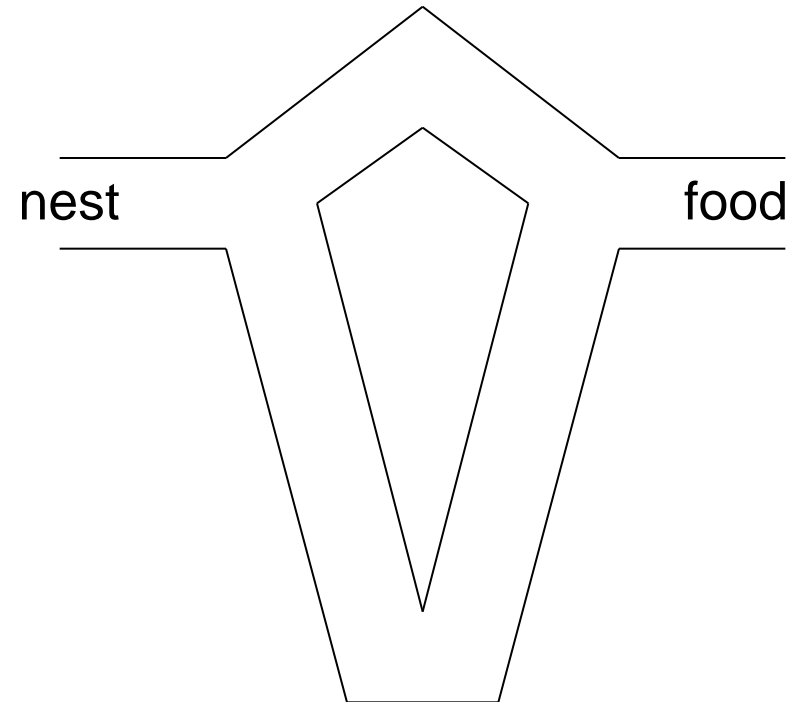


**initially:**

both bridges used equally often

**finally:**

all ants run over single bridge only!



**finally:**

all ants use the **shorter** bridge!

### How does it work?

- ants place pheromons on their way
- routing depends on concentration of pheromons

### more detailed:

ants that use shorter bridge return faster

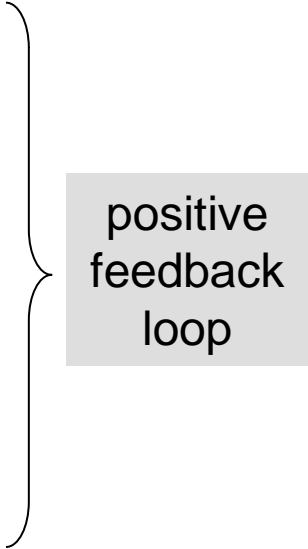
⇒ pheromone concentration higher on shorter bridge

⇒ ants choose shorter bridge more frequently than longer bridge

⇒ pheromon concentration on shorter bridge even higher

⇒ even more ants choose shorter bridge

⇒ a.s.f.



positive  
feedback  
loop

## Ant System (AS) 1991

combinatorial problem:

- components  $C = \{ c_1, c_2, \dots, c_n \}$
- feasible set  $F \subseteq 2^C$
- objective function  $f: 2^C \rightarrow \mathbb{R}$

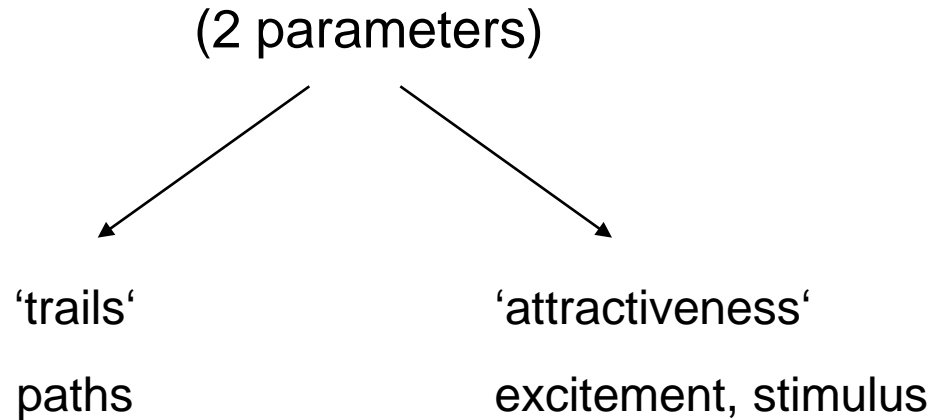
**ants** = set of concurrent (or parallel) asynchronous agents  
move through state of problems



partial solutions of problems

⇒ caused by movement of ants the final solution is compiled incrementally

**movement:** stochastic local decision



while constructing the solution (if possible), otherwise at the end:

1. evaluation of solutions
2. modification of 'trail value' of components on the path



feedback



**ant k in state i**

- determine all possible continuations of current state i
- choice of continuation according to probability distribution  $p_{ij}$

$$p_{ij} = q(\text{attractivity, amount of pheromone})$$



heuristic is based on *a priori*  
desirability of the move



*a posteriori* desirability of the move  
„how rewarding was the move in the past?“

- update of pheromone amount on the paths:  
as soon as all ants have compiled their solutions  
good solution ↗ increase amount of pheromone, otherwise decrease ↘

## Combinatorial Problems (Example TSP)

### TSP:

- ant starts in arbitrary city  $i$
- pheromone on edges  $(i, j)$ :  $\tau_{ij}$
- probability to move from  $i$  to  $j$ : 
$$p_{ij}^{(t)} = \frac{\tau_{ij}^\alpha \eta_{ij}^\beta}{\sum_{k \in \mathcal{N}_i(t)} \tau_{ik}^\alpha \eta_{ik}^\beta} \quad \text{for } j \in \mathcal{N}_i(t)$$
- $\eta_{ij} = 1/d_{ij}$ ;  $d_{ij}$  = distance between city  $i$  and  $j$
- $\alpha = 1$  and  $\beta \in [2, 5]$  (empirical),  $\rho \in (0,1)$  “evaporation rate“
- $\mathcal{N}_i(t)$  = neighborhood of  $i$  at time step  $t$  (without cities already visited)
- update of pheromone after  $\mu$  journeys of ants: 
$$\tau_{ij} := \rho \tau_{ij} + \sum_{k=1}^{\mu} \Delta \tau_{ij}(k)$$
- $\Delta \tau_{ij}(k) = 1 / (\text{tour length of ant } k)$ , if  $(i,j)$  belongs to tour

### two additional mechanisms:

1. *trail evaporation*
2. *demon actions* (for centralized actions; not executable in general)

Ant System (AS) is prototype

tested on TSP-Benchmark → not competitive

⇒ but: works in principle!

subsequent: 2 targets

1. increase efficiency (→ competitiveness with *state-of-the-art* method)
2. better explanation of behavior

1995 ANT-Q (Gambardella & Dorigo), simplified: 1996 ACS *ant colony system*

### Particle Swarm Optimization (PSO)



abstraction from fish / bird / bee swarm

paradigm for design of metaheuristics for continuous optimization

developed by Russel Eberhard & James Kennedy (~1995)

#### concepts:

- particle  $(x, v)$  consists of position  $x \in \mathbb{R}^n$  and “velocity” (i.e. direction)  $v \in \mathbb{R}^n$
- PSO maintains multiple potential solutions at one time
- during each iteration, each solution/position is evaluated by an objective function
- particles “fly” or “swarm” through the search space  
to find position of an extremal value returned by the objective function

## PSO update of particle ( $x_i, v_i$ ) at iteration $t$

1st step:

$$v_i(t+1) = \omega v_i(t) + \gamma_1 R_1 (x_b^*(t) - x_i(t)) + \gamma_2 R_2 (x^*(t) - x_i(t))$$

↓  
const.

↓  
const.

↓  
random  
variable

↓

best solution  
among all solutions  
of iteration  $t \geq 0$

$$x_b^*(t) = \operatorname{argmin}_{i=1, \dots, \mu} \{f(x_i(t))\}$$

↓  
const.

↓  
const.

↓  
random  
variable

↓

best solution  
among all solutions  
up to iteration  $t \geq 0$

$$x^*(t) = \operatorname{argmin}_{\tau=0, \dots, t} \{f(x_b^*(\tau))\}$$

## PSO update of particle ( $x_i$ , $v_i$ ) at iteration $t$

1st step:

$$v_i(t+1) = \omega v_i(t) + \gamma_1 R_1 (x_b^*(t) - x_i(t)) + \gamma_2 R_2 (x^*(t) - x_i(t))$$



new  
direction



old  
direction



direction from  
 $x_i(t)$  to  $x_b^*(t)$



direction from  
 $x_i(t)$  to  $x^*(t)$

- $\omega$  : inertia factor, often  $\in [0.8, 1.2]$
- $\gamma_1$  : cognitive factor, often  $\in [1.7, 2.0]$
- $\gamma_2$  : social factor, often  $\in [1.7, 2.0]$
- $R_1$  : positive r.v., often  $r_1 \sim U[0, 1]$
- $R_2$  : positive r.v., often  $r_2 \sim U[0, 1]$

## PSO update of particle ( $x_i, v_i$ ) at iteration $t$

2nd step:

$$\underbrace{x_i(t+1)}_{\text{new position}} = \underbrace{x_i(t)}_{\text{old position}} + \underbrace{v_i(t+1)}_{\text{new direction}}$$

Note the similarity to the concept of mutative step size control in EAs: first change the step size (direction), then use changed step size (direction) for changing position.

### **More swarm algorithms:**

- Artificial Bee Colony
- Krill Herd Algorithm
- Firefly Algorithm
- Glowworm Swarm
- ...

### **But be watchful:**

Is there a new algorithmic idea inspired from the biological system?

Take a look at the code / formulas: Discover similarities & differences!

Oftentimes: “Old wine in new skins.”