

• Ant algorithms

Particle swarm algorithms

Swarm Intelligence

(optimization in \mathbb{R}^n)

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(combinatorial optimization)

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Swarm Intelligence

metaphor

swarms of bird or fish ants or termites
seeking for food seeking for food

stigmergy = indirect communication through modification of environment

 \sim 1991 Colorni / Dorigo / Maniezzo: Ant System (also: 1. ECAL, Paris 1991) Dorigo (1992): collective behavor of social insects (PhD)

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Swarm Intelligence

ante:

ant algorithms (ACO: Ant Colony Optimization)

paradigm for design of metaheuristics for combinatorial optimization

some facts:

• about 2% of all insects are social

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about 50% of all social insects are ants

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total weight of all ants = total weight of all humans

• humans populate
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ants populate earth since 100 millions years
humans populate earth since 50.000 years

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conspecifics

concepts:

evaluation of own current situation

comparison with other conspecific

• imitation of behavior of successful

⇒ audio-visual communication

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concepts:

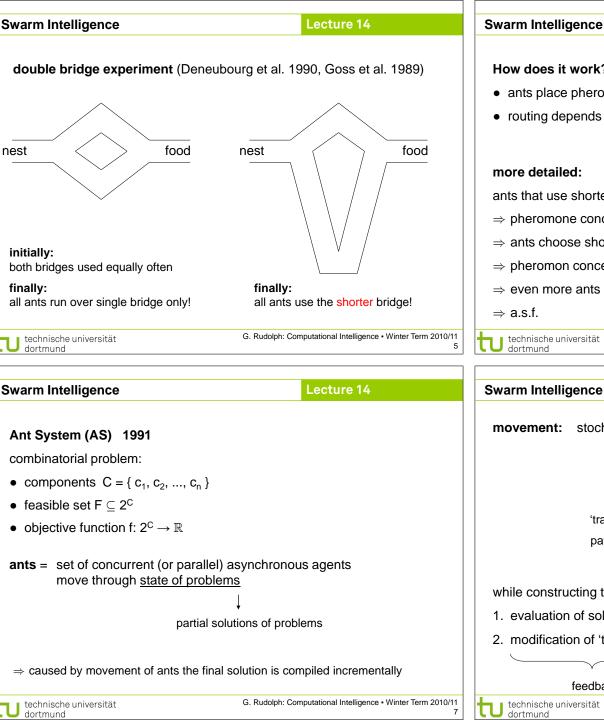
• communication / coordination

⇒ olfactoric communication

by means of "stigmergy"

• reinforcement learning

→ positive feedback



routing depends on concentration of pheromons more detailed: ants that use shorter bridge return faster ⇒ pheromone concentration higher on shorter bridge ⇒ ants choose shorter bridge more frequently than longer bridge ⇒ pheromon concentration on shorter bridge even higher ⇒ even more ants choose shorter bridge \Rightarrow a.s.f. G. Rudolph: Computational Intelligence • Winter Term 2010/11 technische universität Lecture 14 **Swarm Intelligence** movement: stochastic local decision (2 parameters) 'trails' 'attractiveness' paths excitement, stimulus

while constructing the solution (if possible), otherwise at the end:

2. modification of 'trail value' of components on the path

1. evaluation of solutions

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feedback

How does it work?

ants place pheromons on their way

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positive

feedback

loop

ant k in state i determine all possible continuations of current state i • choice of continuation according to probability distribution pi $p_{ii} = q(attractivity, amount of pheromone)$ heuristic is based on a priori a posteriori desirability of the move desirability of the move "how rewarding was the move in the past?" update of pheromone amount on the paths: as soon as all ants have compiled their solutions good solution → increase amount of pheromone, otherwise decrease \ technische universität G. Rudolph: Computational Intelligence • Winter Term 2010/11 Lecture 14

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Swarm Intelligence

Swarm Intelligence

trail evaporation

Ant System (AS) is prototype

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two additional mechanisms:

demon actions (for centralized actions; not executable in general)

tested on TSP-Benchmark → not competitive ⇒ but: works in principle!

subsequent: 2 targets

1. increase efficiency (→ competitiveness with state-of-the-art method)

2. better explanation of behavior 1995 ANT-Q (Gambardella & Dorigo), simplified: 1996 ACS ant colony system

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• $\eta_{ii} = 1/d_{ii}$; $d_{ij} = distance$ between city i and j

• α = 1 and $\beta \in [2, 5]$ (empirical), $\rho \in (0,1)$ "evaporation rate" • $\mathcal{N}_i(t)$ = neighborhood of i at time step t (without cities already visited)

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Swarm Intelligence

Swarm Intelligence

 ant starts in arbitrary city i pheromone on edges (i, j): τ_{ii}

TSP:

Particle Swarm Optimization (PSO)

Combinatorial Problems (Example TSP)

• $\Delta \tau_{ii}(k) = 1$ / (tour length of ant k), if (i,j) belongs to tour

 $\bullet \text{ probability to move from i to j:} \quad p_{ij}^{(t)} = \frac{\tau_{ij}^{\alpha}\,\eta_{ij}^{\beta}}{\sum\limits_{k\in\mathcal{N}:(t)}\tau_{ik}^{\alpha}\,\eta_{ik}^{\beta}} \quad \text{for } j\in\mathcal{N}_i(t)$

• update of pheromone after μ journeys of ants: $\tau_{ij} := \rho \, \tau_{ij} + \sum_{i} \Delta \tau_{ij}(k)$

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abstraction from fish / bird / bee swarm paradigm for design of metaheuristics for continuous optimization

particles "fly" or "swarm" through the search space

to find position of an extremal value returned by the objective function

• particle (x, v) consists of position $x \in \mathbb{R}^n$ and "velocity" (i.e. direction) $v \in \mathbb{R}^n$

• PSO maintains multiple potential solutions at one time

• during each iteration, each solution/position is evaluated by an objective function

developed by Russel Eberhard & James Kennedy (~1995)

concepts:

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Lecture 14 Swarm Intelligence PSO update of particle (x_i, v_i) at iteration t 1st step: $v_i(t+1) = \omega v_i(t) + \gamma_1 R_1 (x_b^*(t) - x_i(t)) + \gamma_2 R_2 (x^*(t) - x_i(t))$ const. const. const. random random variable variable best solution best solution among all solutions among all solutions of iteration $t \ge 0$ up to iteration $t \ge 0$ $x_h^*(t) = \operatorname{argmin} \{ f(x_i(t)) \}$ $x^*(t) = \operatorname{argmin} \{ f(x_h^*(\tau)) \}$ $i = 1, ..., \mu$ G. Rudolph: Computational Intelligence • Winter Term 2010/11 technische universität

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PSO update of particle (x_i, v_i) at iteration t

2nd step:

 $x_i(t+1) = x_i(t) + v_i(t+1)$ new old new position position direction

Note the similarity to the concept of mutative step size control in EAs: first change the step size (direction), then use changed step size (direction) for changing position.

PSO update of particle (x_i, v_i) at iteration t

Swarm Intelligence

new old direction from direction direction $x_i(t)$ to $x_h^*(t)$ $x_i(t)$ to $x^*(t)$

 $\begin{array}{ll} \sigma & : & \text{inertia factor, often} \in [0.8, 1.2] \\ 1 & : & \text{cognitive factor, often} \in [1.7, 2.0] \\ 2 & : & \text{social factor, often} \in [1.7, 2.0] \end{array}$

 R_1 : positive r.v., often $r_1 \sim U[0,1]$ R_2 : positive r.v., often $r_2 \sim U[0,1]$

 n_2 . positive r.v., orten $r_2 \sim \partial r_0$

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