

The (μ, λ) -ES

One generation transition function ((μ, λ) -selection):

$$opt_{(\mu, \lambda)-ES}(P^{(t)}) = \text{sel}_{\mu}^{\lambda}(\sqcup_{i=1}^{\lambda} \{\text{mut}(\text{rec}(P^{(t)}))\})$$

ALGORITHM 2 $((\mu, \lambda)$ -ES)

```

 $t := 0;$ 
initialize  $P^{(0)} = \{\vec{a}_1, \dots, \vec{a}_{\mu}\} \in I^{\mu}$ ;
evaluate  $f(\vec{x}_1), \dots, f(\vec{x}_{\mu})$ ;
while  $(T(P^{(t)}) = 0)$  do
     $\tilde{P} := \emptyset$ ;
    for  $i := 1$  to  $\lambda$  do
         $(\tilde{\vec{x}}, \tilde{\vec{\sigma}}, \tilde{\vec{\alpha}}) := \text{mut}(\text{rec}(P^{(t)}))$ ;
        evaluate  $f(\tilde{\vec{x}})$ ;
         $\tilde{P} := \tilde{P} \sqcup \{(\tilde{\vec{x}}, \tilde{\vec{\sigma}}, \tilde{\vec{\alpha}})\}$ ;
    od
     $P^{(t+1)} := \text{sel}_{\mu}^{\lambda}(\tilde{P})$ ;
     $t := t + 1$ ;
od

```

For $(\mu + \lambda)$ -selection:

$$opt_{(\mu+\lambda)-ES}(P^{(t)}) = \text{sel}_{\mu}^{\mu+\lambda}(\sqcup_{i=1}^{\lambda} \{\text{mut}(\text{rec}(P^{(t)}))\} \sqcup P^{(t)})$$