

The (1 + 1)-ES

- $\mu = \lambda = 1$, no recombination.
- Individual structure: $\vec{a} = (\vec{x}, \sigma) \in I\!\!R^n \times I\!\!R_+$.
- Mutation: 1/5-success rule

$$\tilde{\sigma} := \text{mu}_\sigma(\sigma) = \begin{cases} \sigma / \sqrt[n]{c} & , \text{ if } p > 1/5 \\ \sigma \cdot \sqrt[n]{c} & , \text{ if } p < 1/5 \\ \sigma & , \text{ if } p = 1/5 \end{cases}$$

$$\tilde{\vec{x}} := \text{mu}_{\vec{x}}(\vec{x}) = (x_1 + z_1, \dots, x_n + z_n)$$

- p denotes the measured relative frequency of successful mutations.
- $c = 0.817$ proposed by Schwefel.
- $z_i \sim N_i(0, \tilde{\sigma}^2)$.

- Selection:

$$\text{sel}_1^2(\{\vec{a}, \tilde{\vec{a}}\}) = \begin{cases} \{\tilde{\vec{a}}\} & , \text{ if } f(\tilde{\vec{x}}) \leq f(\vec{x}) \\ \{\vec{a}\} & , \text{ otherwise} \end{cases} .$$

- Generation transition:

$opt_{(1+1)-ES}(\{\vec{a}\}) = \text{sel}_1^2(\{\text{mut}(\vec{a})\} \sqcup \{\vec{a}\})$