

Notation

- Individual: $\vec{a} \in I$.
- Individual space: $I = IR^n \times S$.
- Strategy parameters: S .
- Population: $P^{(t)} = \{\vec{a}_1, \dots, \vec{a}_n\} \in I^k$, $k \in \{\mu, \lambda\}$.
- Recombination: $\text{rec} : I^\mu \rightarrow I$.
- Mutation: $\text{mut} : I \rightarrow I$.
- Selection: $\text{sel}_\mu^k : I^k \rightarrow I^\mu$, $k \in \{\lambda, \mu + \lambda\}$.
- Generation transition: $opt_{ES}(P^{(t)}) : I^\mu \rightarrow I^\mu$

$$opt_{ES}(P^{(t)}) = \text{sel}_\mu^k(\sqcup_{i=1}^\lambda \{\text{mut}(\text{rec}(P^{(t)}))\} \sqcup Q)$$

$$(k = \lambda + |Q|, Q \in \{P^{(t)}, \emptyset\}).$$

- Realization of a normally distributed random variable:
 $z \sim N(\zeta, \sigma^2)$.

Random number generation:

$$z_1 = \sqrt{-2 \ln u_1} \sin(2\pi u_2) \quad , \quad z_2 = \sqrt{-2 \ln u_1} \cos(2\pi u_2)$$

$$u_1, u_2 \sim U((0, 1]), z_1, z_2 \sim N(0, 1).$$